

# OBTAINING THE VOCAL-TRACT AREA FUNCTION FROM THE VOWEL SOUND

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## 1. INTRODUCTION

Vocal-tract area functions (VTAFs) are needed in speech synthesis, speech recognition, and the detection of the vocal-tract shape. The vocal-tract area function can be measured using X-ray or MRI methods. But, both methods are time-consuming and not convenient. It has long been desired to obtain the vocal-tract area function from the speech signal.

It is shown that the VTAF can be derived from the vocal-tract filter (VTF) assuming the wall of the vocal tract is rigid, the length of the vocal tract is known, and the lip or the glottal reflection coefficient is 1 [1,2]. In Atal's method for deriving the VTAF from the VTF, the vocal tract is assumed to completely close at the glottis, and to be terminated with characteristic impedance at the lip opening [1]. In Wakita's method, the vocal tract is assumed to be terminated with characteristic acoustic impedance at the glottal end, and with zero acoustic impedance at the lip opening [2]. However, these assumptions about the boundary conditions cannot be satisfied all the times. The glottal reflection coefficient is time varying, because the glottis opens and closes periodically during voicing. The lip radiation impedance can only be approximated as zero at low frequencies, and can be characteristic impedance only when the lip opening is connected with a reflectionless tube.

Accurate estimation of the VTAF requires the VTF estimated from a vowel signal should not contain the influence of the glottal wave, and the influence of the non-ideal glottal and lip boundary conditions. The method for eliminating the influence of the glottal wave on the VTF estimation from a vowel sound signal is developed in [3]. In this paper, we investigate the effect of non-ideal glottal and lip boundary conditions on the estimation of the VTAF.

## 2. THE VOCAL-TRACT FILTER

The acoustic effect of the vocal tract can be modeled using a multi-sectional cylindrical tube, with each section having the same length and different cross-sectional area (Fig.1). The signal flow diagram from the glottal wave  $U_g$  to the lip volume velocity  $U_{lip}$  can be represented in terms reflection coefficient  $r_i$  and the delay  $D$  in each section,  $r_g$  (the glottal reflection coefficient), and  $r_{lip}$  (the lip

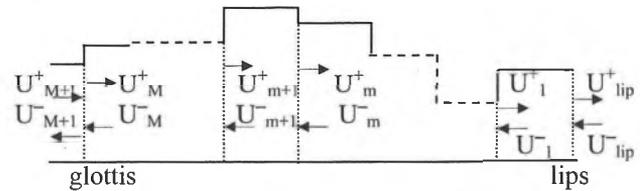


Fig. 1. The acoustic tube model of the vocal tract.

reflection coefficient), as shown in Fig. 2 [3], where  $r_{lip}$  is:

$$r_{lip} = (\rho c / A_1 - Z_{lip}) / (\rho c / A_1 + Z_{lip}) \quad (1)$$

where  $Z_{lip}$  is the lip radiation impedance,  $A_1$  is the cross-sectional area of section 1, and  $\rho c$  is the characteristic impedance of the air.  $r_g$  is defined as:

$$r_g = (Z_g - \rho c / A_M) / (Z_g + \rho c / A_M) \quad (2)$$

where  $Z_g$  is the acoustic glottal impedance,  $A_M$  is the cross-sectional area of section M,

The transfer function from the glottal wave to the lip volume velocity is an all-pole filter, which is denoted as  $TF_{GL}$ . It is time varying due to the time varying  $r_g$ . The all-pole filter estimated from speech signals using LPC [1] is usually called as vocal-tract filter. But, it is actually an averaged version of the  $TF_{GL}$ , and is some different from what is required in the estimation of the VTAF. In Atal's method, the VTF used for estimating the VTAF is defined to be the complex ratio of the total volume velocity at the lips to the total volume velocity at the backend of the vocal tract, i.e.,  $U_{lip} / (U_M^+ + U_M^-)$ . The  $TF_{GL}$  is identical to the VTF in Atal's method, only if  $r_g=1$ . In Wakita's method, the VTF is defined to be the complex ratio of the total volume velocity at the lips to the volume velocity entering the glottis from the trachea, i.e.,  $U_{lip} / U_{M+1}^+$ , assuming  $Z_{lip}=0$ , i.e.,  $r_{lip}=1$ . The  $TF_{GL}$  is identical to the VTF in Wakita's method, only if  $r_{lip}=1$ .

## 3. VOCAL-TRACT BOUNDARY CONDITIONS AND VOCAL-TRACT AREA FUNCTION ESTIMATION

In order to see the effect of non-ideal  $r_g$  and  $r_{lip}$  contained in the  $TF_{GL}$  on the estimation of the VTAF, we synthesize the  $TF_{GL}$  for a given VTAF, and different  $r_{lip}$ 's and  $r_g$ 's, and use the synthetic  $TF_{GL}$  to estimate the VTAF. The difference between the estimate and the given VTAF is

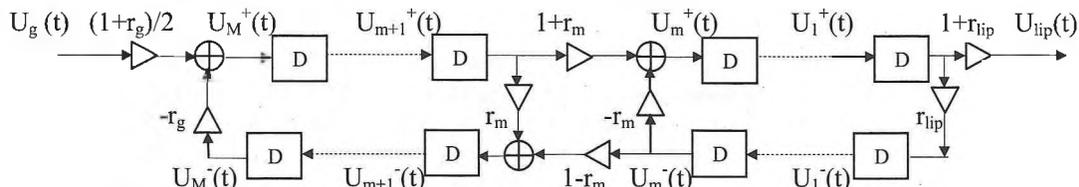


Fig. 2. The signal flow diagram from the glottal wave to the lip volume velocity.

the effect of the non-ideal  $r_g$  and  $r_{lip}$ . The VTAF of /a/ measured using the magnetic resonance imaging method [4] is used in synthesizing the impulse response of the  $TF_{GL}$ . From the synthetic impulse response, we estimate the VTAF under different assumptions about the vocal-tract boundary conditions. If the vocal-tract boundary conditions are assumed to be  $r_g=1$  and  $r_{lip}$  is arbitrary, the vocal-tract reflection coefficients are estimated using method 1:

$$r_m = -k_{m-1} \quad m=1,2,\dots,M-1 \quad (\text{method 1})$$

where  $r_m=(S_m-S_{m+1})/(S_m+S_{m+1})$ ,  $S_m$  is the cross-sectional area of section  $m$ ,  $m$  increases from the glottis to the lips,  $k_m$  is defined in Eq. (11) in [2]. This method is derived through matching Atal's acoustic filtering process [1] to Wakita's mathematical filtering process of the VTF [2]. If the vocal-tract boundary conditions are assumed to be  $r_{lip}=1$  and  $r_g$  is arbitrary, the vocal-tract reflection coefficients are estimated using method 2:

$$r_m = k_{m-1} \quad m=1,2,\dots,M-1 \quad (\text{method 2 [2]})$$

where  $m$  increases from the lips to the glottis [2]. Let  $S_1=1$ , the normalized cross-sectional areas, which form the VTAF, are then obtained:

$$S_{m+1}=S_m(1-r_m)/(1+r_m) \quad m=1,2,\dots,M-1 \quad (3)$$

The frequency responses of the synthetic  $TF_{GL}$ 's and the VTAF estimates derived from the synthetic  $TF_{GL}$ 's using methods 1 and 2 for /a/ are shown in Fig. 3. The bandwidths of the resonance of the VTF are damped, which represent the energy loss in the  $TG_{GL}$ , if  $r_g$  or  $r_{lip}$  is small. The influence of the glottal loss and lip loss on the estimation of the VTAF can be seen comparing the estimates with the given VTAF used for synthesizing the VTF. Our results show that the VTAF can be recovered from the  $TF_{GL}$  using method 1, if the  $TF_{GL}$  corresponds to  $r_g=1$ ; or, using method 2, if the  $TF_{GL}$  corresponds to  $r_{lip}=1$ . Method 1 works well only if the glottal reflection coefficient is one, not being affected by different lip reflections. Method 2 works well only if the lip reflection coefficient is one, not being affected by different glottal reflections.

#### 4. DISCUSSION

Although method 2 is not sensitive to  $r_g$ , it is sensitive to  $r_{lip}$ .  $r_{lip}=1$  (i.e.  $Z_{lip}=0$ ) is true for  $ka \ll 1$ , where  $k=2\pi f/c$ ,  $a$  is the lip opening radius. Therefore, only low sampling rate ( $F_s < 7$  kHz) should be used in method 2. The sampling rate  $F_s$  determines the number of sections of the tube model:  $M=2LF_s/c$ , where  $L$  is the length of the vocal

tract, and  $c$  is the sound speed. Thus, method 2 cannot obtain detailed structures of the VTAF.

Method 1 is not subject to  $r_{lip}$ . Therefore, it can work well over wide frequency range, and can allow high sampling rate. Thus, method 1 can obtain more detailed structures of the VTAF than method 2. For more accurate estimation of the VTAF, the  $TF_{GL}$  used in method 1 should be estimated from the speech signal recorded during closed phases of the glottis, and the speech signal should be recorded in a reflectionless tube connected to the lip opening.

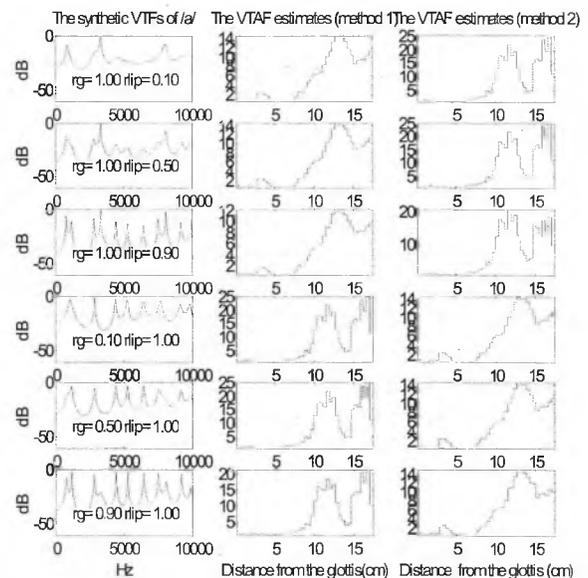


Fig. 3. The synthetic  $TF_{GL}$ 's and the estimates of the VTAF.

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